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for the FOPI collaboration

Velocity correlations of intermediate mass fragments produced in central collisions of Au + Au at $E = 150$ A·MeV
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Abstract: Velocity correlations of intermediate mass fragments (IMFs), produced in central collisions of Au + Au at 150 A-MeV beam energy, are extracted from measurements with the FOPI (phase I) detector system at SIS in GSI Darmstadt. The IMF correlation function for semicentral events is found to be affected by the directed sideward flow. When rotating the events into a unique reaction plane an enhancement of correlations, resulting from event mixing effects, vanishes. Selecting violent collisions with a high degree of azimuthal symmetry the correlation function appears nearly independent of additional event or single particle gate conditions. The comparison of the data with a Coulomb dominated final-state interaction model points to time scales of $\tau \sim 25 \text{ fm/c}$ or less for emitting IMFs from an expanding and multifragmenting source with radius $R \sim 14 \text{ fm}$.
Nuclear intensity interferometry supplies informations on disassembling excited nuclear matter produced in heavy ion collisions. The space-time structure of the source which emits the reaction products can be explored by analysing velocity correlations. This has been exploited for various kinds of particles produced in different reactions [1]. Intermediate mass or heavy fragments mainly undergo final state Coulomb interaction, which prevents the proximity of such fragments in momentum space. Therefore, the appearance of small velocity differences of fragments is suppressed, in particular for small and/or short-living sources.

The analysis of velocity correlations of intermediate mass fragments (IMFs) with charges $Z \geq 3$ emitted in asymmetric heavy ion reactions at beam energies $E < 100$ A·MeV and in more symmetric reactions at beam energies of some tens A·MeV point to considerable life times of the IMF emitting source of the order of a few hundred fm/c [1 - 4]. This has been interpreted as indication of a sequential decay of the primordial (compound-nucleus like) system. On the other hand, theoretical models predict the dominance of a more instantaneous decay of the primordial fire ball into IMFs and light particles in reactions of heavy nuclei at $E \approx 100$ A·MeV and larger [5, 6]. (The possibility of fast multifragmentation caused by high-energy light projectiles is matter of debate [7, 8].)

In this work we analyse small-angle, small-relative-velocity correlations of IMFs. We present experimental data and a first interpretation of such two-body observables in central Au + Au collisions at $E = 150$ A·MeV. We use the Coulomb suppression of small relative velocities of neighbouring IMFs to get information on the space-time structure of the source.

The data are taken by the highly-granular, azimuthally symmetric "outer plastic wall" of the FOPI detector system at the heavy ion synchrotron SIS at GSI Darmstadt which is well-suited for measuring velocity correlations. Details of the FOPI detector system can be found in Ref. [9]. The outer wall covers the polar angles of $7^\circ$ to $30^\circ$ with 512 scintillator strips in 8 radial sectors. Charge and velocity of the products are provided by $\Delta E$-TOF measurement; in addition polar and azimuthal angles are determined. Ionization chambers in front of the outer plastic wall deliver the $\Delta E$ information and hence the charge $Z$ of those fragments which are stopped inside the scintillator strips. (Double counting of one and the same particle caused by the small geometrical overlap of two strips or a nuclear reaction of the fragment in the detector material is mainly excluded in off-line analysis.) A helium-filled bag reduces energy losses and interactions of reaction products on their way between target and wall. The measured velocities are corrected for the energy loss in different media passed by the particles, including the target itself, which has a thickness of 0.5 % interaction probability. Energy thresholds of the detector system are given by $E_{\text{min}} \approx 15 - 50$ A·MeV for particles with charge $Z = 1 - 15$. The polar angle resolution is determined by the strip front height of 2.4 cm corresponding to $\Delta \Theta = 0.36^\circ$. The position resolution $\sigma(POS)$ along the scintillator strips is related to the mean-timing resolution $\sigma(\text{TOF}) \leq 0.20$ ns by $\sigma(POS) = v_{eff} \cdot \sigma(\text{TOF}) \leq 3$ cm, with $v_{eff}$ being the effective
signal velocity along the strip. Relying on these values the relative-velocity resolution is estimated as $\sigma(v_{12}) \leq 0.005 \, c$ for $Z_1 = Z_2 = 3$ fragments.

Events are classified by different binning procedures. Besides the IMF multiplicity we use the multiplicity of all charged particles seen in the outer plastic wall. Its distribution shows the typical flat plateau and a steep fall-off at higher multiplicities. It is divided into five bins PM1 - PM5. The highest-multiplicity bin PM5 starts at half the plateau value corresponding to an integrated cross section of 350 mb and a maximum impact parameter of 3.3 fm in sharp cut-off approximation [10]. The remaining multiplicity range is subdivided into four equally spaced intervals. The double selection of small values $D < 0.2$ (which defines the cut D1) of the transverse momentum directivity $D = |\sum_i p_{xi,i}|/|\sum_i |p_{xi,i}|$ together with the high multiplicity cut PM5 can be used to select high-centrality events, however, at the cost of a further reduction of the integrated cross section down to a value of 56 mb. Finally, the event-wise determined ratio of transverse-to-longitudinal sum energies $E_{rat} = \sum_i p_{xi,i}^2/\sum_i p_{xi,i}^2$ (assuming $M_i = 2Z_im_N$) is found to be a much more effective centrality measure [11, 12]. Already the single cut ERAT5 defined by $E_{rat} > 0.74$ with about the same integrated cross section as in PM5 selects a pronounced IMF source at midrapidity, in a very similar way as the double cut PM5&D1 does on a much less statistical level. Supplementing informations on one-body observables and event characterization can be found in Refs. [10 - 15].

The observed average IMF number per event $<M_{IMF}>$ is 1.5 (3.6) at charged particle multiplicity 17 (25) seen in the outer wall and rises continuously to 4.3 in PM5 where it seems to saturate. We have analysed a total of about $8 \cdot 10^5$, $9 \cdot 10^4$, $2 \cdot 10^4$ IMF pairs in the event classes PM3 - PM5, ERAT5, PM5&D1 and $7 \cdot 10^4$ pairs within an additional gate on the midrapidity region $y \sim y_{c.m.s.} = y_{proj} - y_{c.m.s.}$ PM5, respectively. Correlations of $Z_1 = Z_2 = 2$ clusters with prominent peaks at the known positions of the particle-unstable states $^8$Be(g.s.), $^8$Be(3.04 MeV), and $^9$Be(2.43 MeV), which decay into two $\alpha$-particles, lend credibility to our data processing.

Let $Y_{12}(\vec{v}_1, \vec{v}_2)$ be the coincidence yield of IMF pairs with charges $Z_{1,2}$ and velocities $\vec{v}_{1,2}$. Then the two-particle correlation function is defined as [1]

$$1 + R_{12}(\vec{v}_1, \vec{v}_2) = N \frac{\sum_{\text{events pairs}} Y_{12}(\vec{v}_1, \vec{v}_2)}{\sum_{\text{events pairs}} Y_{12, \text{mix}}(\vec{v}_1, \vec{v}_2)}.$$  \hfill (1)

The sum runs over all events and pairs fulfilling certain selection criteria (see below). Event mixing, denoted by the subscript "mix", means to take IMF #1 and IMF #2 out of different events. We only mix events found within the same event class. $N$ is a normalization factor fixed by the requirement to have the same number of true and mixed pairs. The correlation function (1) is projected onto the hypersurface $v_{12} = |\vec{v}_{12}| = |\vec{v}_1 - \vec{v}_2|$. Besides the above mentioned global event characteristics we use gate conditions on the pair rapidity $y = \frac{1}{2}(y_1 + y_2)$, on the pair velocity $V_{12} = |\vec{V}_{12}| = \frac{1}{2}|\vec{v}_1 + \vec{v}_2|$, or on the angle $\xi$ between $\vec{v}_{12}$ and $\vec{V}_{12}$.
Mutual Coulomb repulsion within an IMF pair results in the scaled asymptotic relative velocity

$$v_{\text{red}} \equiv \frac{v_{12}}{\sqrt{Z_1 + Z_2}} = \left[v_{\text{red},0}^2 + \frac{e^2}{m_N d_0}\right]^{1/2}$$

where the IMF mass numbers are $A_{1,2} = 2Z_{1,2}$, and the "initial" relative velocity and distance are $v_{12,0}$ ($v_{\text{red},0} = v_{12,0}/\sqrt{Z_1 + Z_2}$) and $d_0$ ($e$ and $m_N$ stand for elementary charge and nucleon mass). Please observe the charge independence of $v_{\text{red}}$ as long as the Coulomb repulsion energy dominates. Indeed, when displaying $1 + R$ vs. $v_{\text{red}}$, instead vs. $v_{12}$, we find that different charge combinations result in rather similar curves [14]. This scaling, predicted in Ref. [16] and first verified experimentally in Ref. [17], is used in the following. It allows for systematical studies of the correlation function even if rather restrictive event-selection criteria are applied. Otherwise, if only certain charge combinations were included the available statistics would be too low.

In Fig. 1 the yields of analysed pairs are displayed as function of the relative velocity and the relative azimuthal angle. In the relative-velocity yield (Fig. 1a) a slight shift towards higher values of $v_{\text{red}}$ is observed when going from PM3 - PM5 to the more central ERAT5 bin. Selecting pairs from the PM5&D1 event class or pairs from the midrapidity region in PM5 events yields a similar distribution as found for ERAT5. The azimuthal distribution is sensitive to the event selection criteria, too (see Fig. 1b). It is discussed in more detail below. Fig. 2 displays the experimental correlation function for all events in PM3 - PM5. In the region $v_{\text{red}} < 0.015$ c the mutual Coulomb repulsion causes the Coulomb suppression. It is located in a region of reduced statistics, as seen in a comparison with Fig. 1a, where the maximum yield is at $v_{\text{red}} \sim 0.06$ c. In contrast to previous experiments [2, 3], but in line with a recent measurement [4], we find an enhancement of correlations at $v_{\text{red}} \sim 0.025$ c (full squares in Fig. 2). When rotating all events into a unique reaction plane before event mixing the enhancement vanishes (see open squares). In this way we believe to eliminate widely an unwanted effect of the sideward directed flow of semi-central collisions (see below for further discussions).

In order to study the influence of the experimental set-up on the correlation function we have performed Monte Carlo simulations with several event generators and the GEANT package [18]. As in the experimental data, we find an enhanced coincidence yield due to double countings at very small relative velocities ($v_{\text{red}} < 0.005$ c) mainly caused by secondary interactions in the scintillator strips. This disturbing yield, which is strongest for peripheral collisions, is reduced drastically by excluding, around a given hit, positions on neighbouring strips within an azimuthal segment of $\Delta \phi = \pm 5^\circ$. This procedure excludes also true hits. However, the simulation allows us to determine a lower relative-velocity limit above which the experimental correlation function is not systematically affected: For $v_{\text{red}} > 0.006$ c the correlation function after filtering by the response of the apparatus (the finite angular, velocity and charge resolutions, the energy thresholds and the exact geometry), suffers only minor distortions.
We have studied the dependence of the correlation function on various event characteristics and gate conditions and find the following results when rotating all events into a unique reaction plane before mixing (Naturally, the event rotation does not have any influence on the mixing procedure if subgroups of azimuthally symmetric (i.e. low directivity) events are selected.):

(i) There is no obvious dependence on IMF multiplicity observed in the outer wall acceptance.

(ii) A slight dependence on the charged particle multiplicity of the Coulomb suppression, which is stronger for higher multiplicities, is attributed to the residual influence of sideward directed flow in PM3 - PM5 events after their rotation into a unique reaction plane. (Because of finite particle number effects the reaction plane determination is associated with a finite dispersion of typically $30^\circ - 40^\circ$ for PM4 events.)

(iii) Longitudinal and transversal correlation functions (i.e., pairs with $\xi = 0^\circ - 30^\circ / 150^\circ - 180^\circ$ and $\xi = 70^\circ - 110^\circ$) do not differ significantly. However, they would show a strong splitting if the event rotation into a unique reaction plane is not performed.

(iv) The Coulomb suppression is stronger for central events selected by ERAT5 (see Fig. 3); no significant further shift of the correlation function in the considered interval is found if more restrictive $E_{rat}$ conditions are applied or if PM5&D1 events are selected.

(v) Pairs from the midrapidity region $y \sim y_{c.m.s} \pm \frac{1}{2}(y_{proj} - y_{c.m.s})$ in PM5 events show the same correlation function as pairs from the ERAT5 or PM5&D1 events displayed in Fig. 3.

The error bars in Figs. 1 - 3, whenever shown, indicate statistical errors only. In the correlation function the errors are governed by those of the coincidence yield; the mixed yield is generated with an order of magnitude higher statistics.

In order to understand these experimental results and their global dependences we have performed different simulations, the results of which have been filtered through the detector acceptance. The present interpretation is based on calculations of N-body Coulomb trajectories of charged particles which are initially randomly and non-overlappingly distributed in a sphere of radius $R$. Initially, the particles have a Maxwellian velocity distribution characterized by a temperature $T$. A collective radial expansion, with linear velocity profile $v(r) = (r/R)v_{surf}$ (with $v_{surf}$ as adjustable parameter), is superimposed on the random thermal initial motion. After Coulomb evolution the particle ensemble is boosted in longitudinal (to account for the $c.m.s$ motion) and randomly oriented in transverse direction (to mimic transverse directed flow of the forward $c.m.s$ hemisphere particles which mainly are observed in the detector). Typically, $10^5$ events ($\sim 10^6$ IMF pairs within the outer wall acceptance) have been generated for each parameter set.

In the following we show that for central events (characterized here by ERAT5) the parameters of the Coulomb simulation are widely constrained by experimental data: The experimental charge distribution is found to fall off exponentially $dN/dZ \sim \exp(-\alpha Z)$ for central events [19]. The slope parameter $\alpha = 0.8$ and the averaged mult-
tiriplicity $<M_{IMF}> \simeq 4$ of IMFs detected in the outer wall are used to fix the input charge and multiplicity distributions. The radial expansion velocity parameter $v_{surf}$ and the temperature parameter $T$ we fix by the dependence of the averaged kinetic energy per nucleon $<E/A>_{cm}$ vs. fragment mass $A$ (assuming $A=2Z$). Relying on the recent analysis of central events in ERAT5 [12, 15] we use $<E/A>_{flow} = 12$ MeV and $T = 15$ MeV for the collective and randomized particle motion, respectively. The velocity of the radial expansion profile is related to the mean flow energy by $(E/A)_{flow} = \frac{3}{10}m_Nv_{surf}^2$. Thus, the energy parameter translates into $v_{surf} = 0.20$ c. The transverse boost $v_\perp$ is the main variable for reproducing the enhanced correlations observed at $v_{red} \sim 0.025$ c. A systematic analysis of the directed flow [12, 13] shows that on average not more than 1 MeV per nucleon resides in this collective transverse motion (whereas the available mean energy amounts to 37 A·MeV). This restricts the maximum transverse velocity to $v_\perp < 0.045$ c. With the temperature and velocity parameters fixed in this way the experimental coincidence yield, displayed in Fig. 1a, is well reproduced. In Fig. 3 the results of simulations with three different source radius parameters $R$ are overlaid onto the experimental correlation functions. In order to find the optimum source radius (which is now the only remaining free parameter for fitting the Coulomb flank of the correlation function) we perform a $\chi^2$ minimization of the simulated correlation function with respect to the experimental data for IMF pairs from central (ERAT5) events within the relative-velocity range $0.006 \leq v_{red} \leq 0.05$ c. The optimization leads to $R = 14 \pm 2$ fm where the error band corresponds to a deviation of $\sim 1$ from the minimum of $\chi^2$ per degree of freedom (which amounts to 1.8). Finally, we find satisfying agreement with the data in Figs. 1 - 3 with a parameter set for central events (defined by ERAT5)

$$R = 14 \text{ fm}, T = 15 \text{ MeV}, v_{surf} = 0.20 \text{ c}, v_\parallel = v_{cms} = 0.27 \text{ c}, v_\perp = 0,$$

(3)

and with another one for the PM3 - PM5 events dominated by semi-central collisions (including randomly oriented sideward-directed flow and employing a somewhat higher longitudinal boost)

$$R = 14 \text{ fm}, T = 15 \text{ MeV}, v_{surf} = 0.10 \text{ c}, v_\parallel = 0.40 \text{ c}, v_\perp = 0.045 \text{ c}.$$  

(4)

The parameters can be varied separately within an error range of $\sim 10\%$ without an obvious change of the curves in Figs. 1 - 3. An exception represents the random thermal motion parameter $T$ which leads (as a consequence of the strong radial flow) only to minor distortions of the correlation function even when doubling the temperature. With the parameter set (4) we reproduce also the reduction of the enhancement of correlations at $v_{red} \sim 0.025$ c when regarding the reaction plane orientation, here defined by $\vec{v}_\perp$ (see Fig. 2).

The experimental azimuthal IMF pair distribution in Fig. 1b is fairly well described, too. It evolves from a strongly asymmetric one for the mixture of central and semi-central events in PM3 - PM5 to a more isotropic distribution for the central event selection PM5&D1 (triangles). From the simulation analysis the $\sim 25\%$ reduction in yield at small relative angles is found to be not only due to Coulomb suppression but also, though
to somewhat less extent, a result of momentum conservation and of proximity effects of
the extended clusters within the source at the beginning of the radial expansion. The
distribution of midrapidity IMF pairs in PM5 events (cf. stars in Fig. 1b) point to the
selection of an approximately azimuthally isotropic IMF subgroup, too. The distribution
of IMF pairs from ERAT5 events (see the dots in Fig. 1b) ranges in between the former
ones, thus indicating that some sideward flow is still present in this event class [12, 13].
In contrast to the IMF data shown here, the anisotropies of the corresponding relative-
angle distributions of the light charged particles (\( Z_{1,2} < 3 \)) are found to be much less
pronounced. This is attributed to the lower nuclear charges and to the higher
velocities of the random thermal motion of the light particles whereas the velocities of the heavier
clusters are dominated by the flow [12, 15].

It has to be noted that interpretations of the data without rotating the events into
a unique reaction plane (see Fig. 2) within the Koonin-Pratt model [16] would point to
significant source life times [14]. The essential feature to be regarded indeed seems to be
the directed IMF flow. Such collective effects are known to obscure correlation functions
[20].

Although our simulations do not contain explicitly a source life time one can deduce
a typical time scale of the present scenario. Even if we rely on an instantaneous break-up
picture, the particles need some time to leave the initial source volume defined by \( R \).
According to the initial velocity and spatial distribution one expects a characteristic time
constant of less than 100 fm/c. Indeed, counting at different time steps the number of
particles remaining within the sphere of radius \( R \) we find an exponential decrease with
a typical decay time of \( \tau \sim 25 \) fm/c which is mainly determined by the flow. (When
the radial expansion is switched off this time increases to a value slightly above 100
fm/c.) The short time scales found in the present IMF correlation analysis continue the
trend of decreasing source life times with increasing energy deposited in the system. In a
recent communication [21] the authors report on multifragmentation time scales in central
collisions of Ar + Au decreasing from \( \sim 100 \) fm/c to \( \sim 50 \) fm/c when varying the projectile
energy from 35 to 110 A-MeV.

Note that our data interpretation indicates also a strong expansion effect. The ex-
tracted source radius of \( R = 14 \) fm is substantially larger than a 2\( A_{\text{Au}} \) system at nuclear
saturation density \( \rho_0 \). It corresponds to a freeze-out density of \( \rho \simeq 0.2 \rho_0 \). Also this
dilution is dominated by the radial flow: Without the flow (which, however, is needed
to describe the dependence of the averaged energy per nucleon vs. the fragment mass
[12, 15]) the \( R = 10 \) (20) fm correlation function would approximately coincide with the
the \( R = 20 \) (40) fm curve of Fig. 3 including the radial flow. In order to compensate for
this strong shift a source radius, which is about two times smaller than the optimum one
determined above, would be necessary.

One should have in mind that our simulations neglect dynamical correlations prior to
the Coulomb evolution. Such primordial correlations may stem from the early fragment
formation process, which is dealt with in different models [5, 6, 22, 23, 24]. Our two-body IMF observable data may serve as crucial test of such models, in particular of dynamical event generators such as the QMD model [24].

In summary we present small-relative-velocity correlations of IMFs produced in central collisions of Au + Au at 150 A-MeV. The data are compatible with a fast (instantaneous) multifragmentation picture of a radially expanding source created in central collisions. The importance of both radial and directed collective flow for the data interpretation is shown.

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Fig. 1: The coincidence yield as function of reduced relative velocity (a) and azimuthal IMF pair distribution in the forward hemisphere as function of the relative angle (b). Squares, dots, triangles and stars correspond to IMF pairs found under PM3 - PM5, ERAT5, PM5&D1 cuts and midrapidity pairs in PM5 events, respectively (see text for explanation). The dashed and full lines display simulations with (parameter set (4)) and without (parameter set (3)) taking into account the directed flow.
Fig. 2: The IMF correlation function for events in PM3 - PM5 (full squares). The open squares are for the same events, however, they are rotated into a unique reaction plane before mixing. The full (dashed) line depicts the result of Coulomb trajectory simulations using parameter set (4) with (without) randomization of the reaction plane orientation $\vec{u}_\perp$.

Fig. 3: The correlation function for IMF pairs from ERAT5 events (dots) and from the total ensemble of PM3 - PM5 events (squares). The events are rotated into a unique reaction plane before mixing. The dashed, full and dotted lines correspond to simulations with parameter set (3) but $R = 10, 20, 40$ fm, respectively.